

Fleming's Left-Hand rule:

When a **current** flows through a **magnetic field** at an angle, a **force** acts on the wire. The direction of this force is perpendicular to the current and the field, and can be predicted using Fleming's Left-Hand rule.

The size of the force is given by this equation:

$$F = BIl \sin\theta$$

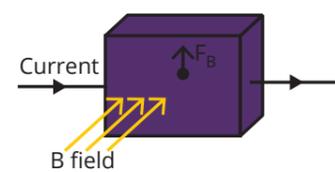
B is the magnetic field strength (or flux density), measured in **Tesla (T)**, where $1 \text{ T} = 1 \text{ N A}^{-1} \text{ m}^{-1}$.

As current is defined as the rate of flow of charge the above equation can be expressed in terms of the force on a single charged particle.

$$F = Bqv \sin\theta$$

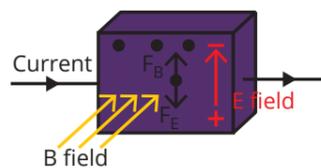
In both equations, θ is the angle between the current and the field lines.

Hall Voltage, V_H :



When a current flows at 90° through a magnetic field, there will be a **force on the electrons** flowing through the wire, forcing them to **one surface** of the conductor. This will cause one surface to become **negative** and the other **positive**.

This creates an electrical field between the surfaces and cause a **force on the electrons in the opposite direction**.



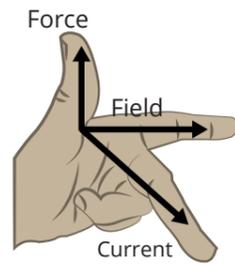
In the end, the magnetic force and the electrical force will **balance** and **an equilibrium is reached**.

$$qE = Bqv$$

As $E = \frac{V}{d}$ this can be written as $V_H = Bvd$ where V_H is the potential difference between the surfaces, measured with a voltmeter, when this equilibrium is reached.

This can be used to measure the strength of B fields as

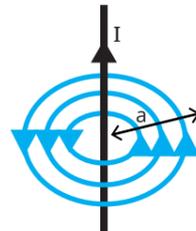
$$B \propto V_H$$



Magnetic fields:

Magnetic fields are created by current carrying wires, the shape of the field can be predicted by the right-hand grip rule.

Long straight wire



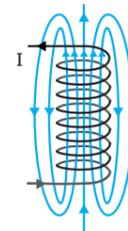
Thumb in the direction of the current, fingers in the direction of the field.

The strength of each field is given by these equations:

$$B = \frac{\mu_0 I}{2\pi a}$$

Where a is the distance from the wire to a point.

Solenoid



Fingers in the direction of the current, thumb in the direction of the field inside the coil.

$$B = \mu_0 n I$$

Where n is the number of turns per meter.

$$n = \frac{\text{number of turns}}{\text{length}}$$

The strength can be increased by using an iron core inside the solenoid.

Parallel wires:

When a current passes through a wire it creates a magnetic field. If two parallel wires carry a current, they will each be in the others magnetic field, therefore a force will act on the wires.



In this example, consider wire X, it creates a magnetic field with strength, $B = \frac{\mu_0 I_X}{2\pi a}$. As wire Y is in this field, the force on wire Y will be $F = BI_Y l$. The direction of the force, given by Fleming's Left-Hand Rule, will be towards wire X.

Newton's 3rd law means that there will also be an equal force on wire X towards wire Y.

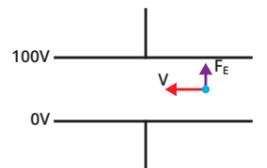
Charged particles in E and B fields:

Any moving charges can be deflected by a magnetic field or an electric field.

Magnetic forces always act perpendicular to the motion. Therefore, the magnetic force acts as a centripetal force and makes the charges move in a circular path.

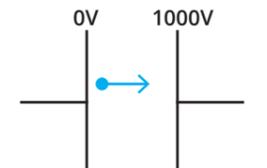
$$Bqv = \frac{mv^2}{r}$$

The **electrical force** between two parallel plates is constant due to the uniform electric field. Therefore, the force acting on the electron here, F_E will cause a vertical acceleration but not change its horizontal velocity.



Particle accelerators:

When a charged particle is accelerated by a potential difference it gains kinetic energy. In this example an electron is accelerated by a p.d. of 1000V, the energy it gains = 1000 eV , where $1 \text{ eV} = 1.6 \times 10^{-19} \text{ J}$.



There are 3 types of particle accelerators which use this process. They all use an alternating p.d. to accelerate the particles in the gaps between electrodes.

| | Linear | Cyclotron | Synchrotron |
|------------------|----------------------------------------------------------------------|-------------------------------------------------------------------|--------------------------------------------------------|
| Path | Straight line | Circular but with increasing radius | Circular, constant radius |
| Magnetic field | None | Constant, to ensure circular motion | Increasing to ensure circular motion with constant r |
| Alternating p.d. | Constant, increasing length of tube ensures the p.d. changes in time | Constant, increasing path length ensures the p.d. changes in time | Increasing |

F = force in N

I = current in A

q = charge in C

n = number of turns per m in m^{-1}

V_H = Hall voltage in V

θ = angle between the current and the field lines in $^\circ$

B = Magnetic field strength in T

l = length in m

v = speed in m s^{-1}

E = Electrical field strength in N C^{-1}

d = plate separation in m